G-band Raman double resonance in twisted bilayer graphene: Evidence of band splitting and folding

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The stacking faults (deviates from Bernal) will break the translational symmetry of multilayer graphenes and modify their electronic and optical behaviors to the extent depending on the interlayer coupling strength. This paper addresses the stacking-induced band splitting and folding effect on the electronic band structure of twisted bilayer graphene. Based on the first-principles density-functional theory study, we predict that the band folding effect of graphene layers may enable the G band Raman double resonance in the visible excitation range. Such prediction is confirmed experimentally with our Raman observation that the resonant energies of the resonant G mode are strongly dependent on the stacking geometry of graphene layers.

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As a semimetal with linear dispersive bands near the Dirac point, graphene, a monolayer of graphite, offers an ideal platform to explore the quasiparticle dynamics within relativistic quantum mechanics. Since its first isolation in 2004,1 graphene has exhibited a series of exceptional properties such as anomalous quantum Hall effects,2,3 absence of weak localization,4,5 the Born-Oppenheimer approximation violation,6 and transport via relativistic massless Dirac fermions.7 However, as a typical two-dimensional material, the electronic properties of graphene are highly sensitive to the number of layers and also the stacking geometry.8 For example, there is band splitting in AB (Bernal) stacked bilayer and few layer graphene, and the electron/hole in such structure is massive.9 Interestingly, the Dirac-type character of electronic states has been revealed recently on multilayer epitaxial graphene on the SiC substrate as well as on large scaled graphene films grown by chemical vapor deposition (CVD), both types of graphene samples were observed to have a high degree of rotational disorder (stacking faults).10–12 Theoretical calculations of electronic structure of twisted bilayer graphene were carried out and showed that the low-energy dispersion of such twisted graphene is linear, similar to that in single-layer graphene (SLG).13,14 The SLG behavior of folded/twisted bilayer graphene has also been demonstrated by Raman spectroscopy.15 In fact, in addition to the decoupling-caused band degeneracy near the Dirac point, the stacking influence may be more significant, as it may break the translational symmetry of graphene and reshape the Brillouin Zone. The obvious result of the shrunk Brillouin zone is that the folded electronic bands that would compress the linear dispersion range of electrons of graphene and therefore limit their Dirac-fermion behaviors. It is also possible that such stacking may remove translation symmetry totally and result in incommensurate structures16 and localized states only. Therefore, two questions arise naturally pertaining to the stacking effect on electronic behaviors of graphene: by how much will the coupling between twisted graphene layers change their electron dispersions and how to measure such changes experimentally.

In this paper, the stacking-dependent band folding and splitting of electronic-dispersion curves of twisted graphene bilayers are clearly revealed with first-principles density-functional theory (DFT) calculations. We propose and confirm for the first time with Raman spectroscopy observation that the normal G band will become double resonant under commensurate stacking which can be a benchmark to evaluate band folding effect in graphene layers.

As a product of semimetal band structure, graphene and graphite exhibit the well-known double resonant Raman (DRR) features.17–19 As DRR requires the intermediate electronic states related to the phonon scattering process be real, the DRR features of graphene/graphite typically come from the disorder-induced D or the two-phonon 2D band rather than the zone-center G band. This disability of G phonons of participating DRR process originates from the constraint of the electronic bands, as will be discussed below. Figure 1 shows the calculated band structure of a bilayer graphene (BLG) with Bernal stacking and a twisted bilayer graphene (rotation angle of 13.2°). Our calculations were performed using the local-density approximation (LDA) within DFT, with the Kohn-Sham equations solved with the projected augmented wave method20 as implemented in the VASP code.21–23 Like SLG, the π and π’ bands of BLG in Fig. 1(a) are overlapped at K point to give a zero band gap.

FIG. 1. (Color online) Electronic band structures of hexagonal graphite (a) and graphene bilayer (b) with rotation angle of 13.2°, with the red and blue arrows indicating the forbidden and allowed electronic transitions for G phonons involved in DRR. The insets are the corresponding atomic structures.
However, within the BLG unit cell the interlayer coupling of electron states modifies their band dispersions and results in band splitting. Considering the exchange operation of the two identical layers, the split $\pi(\pi^*)$ bands will bear even or odd parities, which are noted as $\pi^r(\pi^{r*})$ and $\pi(\pi^*)$ in Fig. 1(a), respectively. According to the selection rule of light absorption and emission, the phonon transition between two electronic bands with different parities are not allowed, because it will result in an prohibited optical transition.\(^{24}\)

Therefore, in BLG the $G$ phonon with energy of 0.196 eV is prohibited to participate into the DRR process excited by visible laser, as schematically indicated by the red arrow in Fig. 1(a). However, such constraint on the $G$ phonon can be removed in twisted graphene layers where the band folding enables the transitions between electron bands with the same parity. Figure 1(b) shows the band structure of a twisted bilayer graphene (rotation angle of 13.2°, unit cell of 76 atoms), with its atomic structure also shown in inset. The electronic bands near the K point are degenerated and exhibit single and linear dispersion, similar to those in SLG. This result agrees well with previous calculations\(^{13,14}\) and explains why the Dirac-type electronic structure is still preserved in multilayer misoriented (twisted) graphene.\(^{11}\) However, the shrunken Brillouin zone shortens the linear dispersion range around the K point and reduces the energy span between conduction and valence states at M point to the visible-light range. Apart from that, clear band splitting is shown along the M-\(\Gamma\) direction, where the $\pi$ and $\pi^*$ bands of single-layer graphene split into $\pi_1^r$, $\pi_1^i$ and $\pi_1^{i*}$ bands, while $\pi_2^r$, $\pi_2^i$ and $\pi_2^{i*}$ bands are brought by the band folding. Such band splitting indicates that the perfect electronic decouple of twisted bilayer graphene only appears near the Dirac point, which was not mentioned in previous theoretical calculations.\(^{11,13,14}\)

Therefore, the electronic structure of twisted bilayer graphene is much more complicated than SLG as well as BLG in the visible energy range. These excessive band features enable the emission of $G$ phonon from a DRR process involving electronic transition excited by visible laser, as schematically indicated by the blue arrow in Fig. 1(b).

While DFT calculations indicate the band folding and splitting effects will modify the electronic structure of twisted graphene significantly and make $G$ band DRR possible, the remaining issue is to demonstrate such changes and phenomena experimentally. In experiment, the graphene samples are prepared by micromechanical cleavage and transferred to Si/SiO$_2$ (~300 nm) substrate.\(^{1}\) The twisted bilayer graphene ($1+1$ layer folded graphene) are prepared by gently flushing deionized water across the surface of the substrate containing the target graphene sheet.\(^{15}\) Some of the graphene sheets are accidentally folded up right after the cleavage.\(^{25}\) As a perfect single-crystalline structure, the graphene sheet is expected to have crystal cleavage behaviors. After studying hundreds of mechanically cleaved graphene, we found that the angles between graphene edges have an average value equaling multiples of 30°, which indicate that the smooth edge of graphene reflects its crystal orientation.\(^{26}\)

The rotation angle between the two layers in folded graphene can then be estimated by knowing the original orientation of SLG. For example, the atomic force microscope (AFM) image of a graphene sheet is shown in Fig. 2(a). The left part is a BLG while the right part is SLG, which are determined by Raman and contrast spectroscopy.\(^{27}\) The triangle area is twisted bilayer graphene. The smooth horizontal edge (dashed black line) indicates the orientation of SLG and BLG, either armchair or zigzag directions. After folding, the orientation of the upper layer is shown by the dashed green line and the twisted angle between the two layers (\(\alpha\)) is estimated from the angle between the dashed green and red lines, which is ~21.2°. The twisted angles of other folded graphene samples are estimated in the similar way. The height along the dashed white line in the AFM image is shown in Fig. 2(b). It can be seen that the height difference between SLG and folded/twisted graphene is ~0.38 nm, similar to the difference between SLG and BLG (~0.35 nm) by considering the experimental error. Therefore, the folded/twisted graphene has similar layer-to-layer distance as BLG, which is adapted in our DFT calculations. The Raman image/spectra are carried out with a WITTEC CRM200 Raman system under 633 (1.96 eV), 532 (2.33 eV), and 457 nm (2.71 eV) excitations. The laser power at sample is below 0.5 mW to avoid laser-induced sample heating. A 100× objective lens with a NA=0.95 is used in the experiments. Details of Raman imaging can be found in Ref. 27.

Figure 3(a) shows an optical image of a SLG sheet. The lower part of the graphene sheet is folded up, whose AFM image shown in Fig. 3(b). In our previous work, a single and symmetric 2D band is observed in such folded sample, i.e.,
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FIG. 3. (Color online) (a) Optical image of a single-layer graphene sheet contains some folded (twisted) regions. (b) AFM image of the sample shown in (a). Raman imaging of the G band intensity of the graphene sample excited by 457 nm (c) and 532 nm (d) lasers, respectively. (e) Raman spectra of folded graphene from area X when excited by 457, 532, and 633 nm laser. (f) Raman spectra of folded graphene from area Y when excited by 457, 532, and 633 nm laser.

FIG. 4. (Color online) (a) The possible resonance process for the Raman G band of graphene. (b) The energy difference of π_z and π_{z'} bands of TBG with rotation angle of 13.2°. (c) The 3D view of the energy difference of π_{s} and π_{s'} bands. (d) The top view of (c).

twisted bilayer graphene, which corresponds to its single and linear Dirac-type electron dispersion. Here, special attention will be paid on the G band of two twisted bilayer graphene, which are labeled as areas X and Y. In area X, the rotation angle between the two layers is ~13°, which is similar to the structure used in the DFT calculations (13.2°) in Fig. 1(b). The Raman spectra of twisted graphene (area X) under 457, 532, and 633 nm excitations are shown in Fig. 3(e). The spectra excited by 532 and 633 nm lasers are normal for graphene, while that excited by 457 nm laser has a very strong G band (~28 times higher than those excited by other lasers. The spectra are normalized using the intensity of SLG under each excitation as a reference). The difference can be seen clearly in the Raman imaging in Fig. 3(c) (457 nm excitation) and Fig. 2(d) (532 nm excitation), which are constructed by the intensity of G band. In the Raman imaging, brighter color represents higher G band intensity. In Fig. 3(c), under 457 nm excitation, the G band intensity of twisted sample (area X) is surprisingly high (~55 times the intensity of SLG). On the other hand, in Fig. 3(d), under 532 nm excitation, the G band intensity of twisted graphene (area X) is only about twice of that of SLG, which is normal for two layer graphene sheet. Therefore, there is a strong G band resonance for twisted bilayer graphene with rotation angle of ~13°, and the resonant laser wavelength is ~457 nm. This is the first observation of strong G band resonance in graphene sheets, and such resonance phenomenon cannot be similar to those observed in carbon nanotubes (CNTs). The resonance of CNTs occurs when the excitation laser energy matches the band gap of CNTs or the energy difference between two quantized electronic levels, while graphene and its multilayers are believed to be semimetal with zero band gap. Another area of interest is the area Y, which has a rotation angle of ~7.5°. It can be seen in Fig. 3(f) that the G band intensity of twisted graphene (area Y) is very high when excited by 532 nm laser, which is almost ~24 times higher than those excited by other lasers, i.e., 457 and 633 nm. This can be also seen from the Raman imaging in Figs. 3(c) and 3(d), where a strong G band resonance at area Y is observed under 532 nm excitation. In addition, a twisted graphene with rotation angle of 21.2° does not show any G resonance phenomenon under all the three excitations (results not shown). Therefore, for twisted bilayer graphene with different rotation angle, the resonance conditions are much different.

DRR requires both incident photon and excited phonon match the real-state electron transitions as illustrated schematically in Fig. 4(a), which shows Stokes DDR process from three π electron states (π_a → π_b → π_a' → π_c). The DDR process will happen only if the energy difference between bands π_a and π_a' (ΔE) is around 0.196 eV (G phonon energy) and the energy of incident laser (E_L) matches the energy difference of bands π_a and π_c. Under such conditions, the whole Raman process is fully resonant, since all intermediate electronic states are real states, therefore, the G band obtained would have an unusually high strength. In the real band structure of twisted bilayer graphene, the electronic bands have different parities, such as π_a(π_{a'}) and π_c(π_{c'}). For example, if we consider the top two valence bands of π_a' and π_{a} and four bottom conduction bands of π_{b'}, π_{b}, π_{b1}, and π_{b2} in Fig. 1(b), one optical transition satisfies the resonant condition for the visible excitations is π_{a} → π_{b} → π_{a'} → π_{c}. Other allowed transitions, such as π_{b1} → π_{b2} → π_{b1} → π_{c}, will require much larger excitation energy (E_L > 3.5 eV). While it is well known that Kohn-Sham eigenvalues of DFT-LDA underestimate the quasiparticle energies, here the calculated transition energy for DRR process has multiplied a calibration parameter of 1.15 following the angle-resolved photoemission spectroscopy and GW results. Figure 4(b) plots the energy difference of π_{c'} and π_{a'} bands of the 13.2° twisted bilayer graphene. The ele-
tronic states satisfying the first requirement of double resonance, $\Delta E = E_{ph} = 0.196$ eV, are labeled with blue cross symbols in Fig. 4(b), and they form some kind of snowflake shape. Another requirement of $G$ band resonance is that the energy of incident laser ($E_l$) matches the energy difference of $\pi_1$ and $\pi_2^*$ bands. Figure 4(c) shows the three-dimensional (3D) view of the energy difference of $\pi_1$ and $\pi_2^*$ bands within the whole Brillouin zone, while Fig. 4(d) gives the top view. The blue crosses in Figs. 4(c) and 4(d) represent the required incident laser energies to excite the electron which also satisfies $\Delta E = E_{ph}$. For those snowflake-shape points qualified for the DRR process, the inner-edge states are preferred for the strong resonance as the small slope of the curve here corresponding to the high joint density of states. Therefore, we estimate the resonant laser energy for the 13.2° twisted bilayer graphene would be about 2.73 eV, which corresponds to a laser wavelength of 454 nm.

In summary, based on first-principles DFT calculations, we demonstrate the stacking dependence of the electronic structure of twisted bilayer graphene, where the band splitting and folding will effectively limit the linear dispersion range of Dirac-fermion electron states and bring more bands to the electronic transitions within the energy range of visible light. Experimental observation of an abnormal strong $G$ band resonance confirms our prediction that the normal $G$ band will become double resonant under right laser energy for the particular stacking geometry of graphene layers. Our results suggest that, in addition to the band degeneracy near the Dirac point, the influence of stacking faults is much more significant on tuning away the optical properties of twisted graphene layers from those of single and multilayer graphene.

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and without water flushing, which indicates water molecular does not play an important role.


