Local structure relaxation, quantum trap depression, and valence charge polarization induced by the shorter-and-stronger bonds between under-coordinated atoms in gold nanostructures

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Relativistic density functional theory calculations have been conducted to examine the effect of atomic under-coordination on the crystal structure, binding energy, and electron configuration of cubo-octahedral and Marks decahedral gold clusters. Trend consistency between calculations and experimental observations confirmed the predictions made using BOLS correlation theory, suggesting that the shorter-and-stronger bonds between under-coordinated atoms induce local structure relaxation, potential well depression, and the associated local charge and energy densification, as well as the polarization of the otherwise conducting s-electrons (valence charge) by the densely- and tightly-trapped core electrons of which the binding energy shifts positively to deeper energies. Findings are in good agreement with scanning tunneling microscopy/spectroscopy results from monomers, dimers, chain ends, and nanostructures of gold and other metals.

1. Introduction

Metallic nanoparticles (NPs) have inspired increasing interest recently because of their intriguing properties that cannot be observed for their bulk counterparts. As the sizes of the NPs decrease, the volume ratio of surface layers to the entire body, called the surface-to-volume ratio, increases up to 90% for a gold NP with a diameter of 1 nm, for instance. The involvement of the interaction between under-coordinated atoms, which distinguishes the NPs from their bulk counterparts in performance, is indeed fascinating. For instance, Au NPs manifest magnetism while the bulk gold is diamagnetic; a phase transition from conductor to insulator occurs at the size of a few nanometres; nanoscale gold meets the demand of local surface plasmons; and the catalytic ability for CO oxidation of gold is greatly enhanced at small sizes. Other intriguing properties for applications include RNA-delivery, localized surface plasma resonance for Raman spectroscopy, laser applications in medicine, enhancement of photoluminescence, etc. Accompanied by the structure evolution from the face-centered-cubic of bulk to strained structures such as icosahedral or decahedral, substantial bond contraction occurs to the outermost few atomic shells, which can be described as an elastic cover sheet of “skin”.

Besides the bond length contraction, the potential trap depth, charge density, energy density, and electronic configurations of the NPs differ from their bulk counterpart as well. Transmission electron microscopy (TEM) measurements have revealed that the inner muffin-tin potential of gold NPs becomes deeper when the particle size is reduced. As a consequence of potential well depression, the Au 4f binding energy, for instance, also goes deeper when the solid dimensions are reduced. A single-electron tunneling spectroscopy experiment revealed the generation of an energy gap whose width is inversely proportional to the diameter of Au NPs and Pd NPs. Meanwhile, the peaks of the valence local density of states (LDOS) of Au monomers and dimers, Au–Au chains, Au nanowires, organic nanowires on Ag substrates, Fe chains on InSe substrates, Cu chains on Cu substrates all move to upper energies as the particle size is reduced. A consistent trend has been observed in trends between calculations and experimental observations on the bond contraction, potential well depression, core level shift, and the valence charge polarization of gold nanostructures. Agreement in trends between calculations and experimental observations confirms the expectations of the bond-order-length-strength...
(BOLS) correlation theory\textsuperscript{30} regarding the performance of the localized edge states. It is stressed that the edge atomic undercoordination induces local strain, quantum trap depression, charge densification and valence charge polarization, which provide perturbation to the Hamiltonian and hence the related properties and observations.

2. Theory: BOLS expectations

Extended from the “atomic coordination-atomic radius” correlation premise of Goldschmidt\textsuperscript{31} and Pauling,\textsuperscript{32} the BOLS correlation\textsuperscript{30,33} deals with under-coordinated systems such as adatoms, defects, edges, grain boundaries, atomic chains, atomic ribbons, atomic tubes, surfaces and nanostructures as an additional inspection to the classical and the quantum approximations. According to the BOLS theory, within skin depth of the outermost atomic shells in the NPs, the curvature $K^{-1}$ (with $K$ being the number of atoms lined along the radius of a spherical dot) dependence of the effective coordination number (CN or $z_e$), bond length ($d_i$), charge density ($n_i$), and the potential trap depth (also bond energy, $E_i$), energy density ($E_id_i^2$) follow the relations:\textsuperscript{30,33}

$$
\begin{align*}
    z_i &= 4(1 - 0.75K^{-1}); z_0 = 12 - z_i \\
    d_i &= 2d(1 + \exp((12 - z_i)/(8z_i)))^{-1} \\
    E_i &= E_0C_i^{-1} \\
    n_i &= nC_i^{-1} \alpha d_i^{-3}
\end{align*}
$$

(1)

The subscript $i$ denotes the $i$th atomic layer counted from the outermost to the center of the sphere and the subscript $b$ represents the corresponding bulk values. Eqn (1) indicates that bonds between under-coordinated atoms at the $i$th shell of NPs will contract spontaneously by $C_i$ associated simultaneously with a $C_i^{-1}$ times bond energy gain. As the consequence of bond contraction and bond energy gain, the local charge density will rise by $C_i^{-3}$ for a three-dimensional specimen and the local potential well will be deepened by $C_i^{-1}$.

By taking the average over the entire nanostructure with a core–shell configuration, the size dependence of the energy density (which is proportional to the elastic modulus\textsuperscript{34}) and potential trap depth (corresponds to the core level shift\textsuperscript{19}) of a specimen,

$$
V(K) = V(\infty) \left[1 + \sum_{i=3}^{n} \gamma_i (C_i^{-1} - 1)\right] \\
\gamma_i = V_i/V = \tau C_i/K
$$

(2)

The parameter $\tau = 3, 2, 1$ represents the dimensionality of a spherical dot, a cylindrical rod and a thin slab, respectively. In eqn (2), the potential trap depth in the surface of up to three atomic layers in depth of a nanostructure is strongly correlated through the bond length and bond energy.\textsuperscript{35}

Increasing experimental evidence\textsuperscript{37,38} favors the quantitative reliability of the BOLS expectation:

(a) Bonds between the under-coordinated atoms become shorter\textsuperscript{31,32} and stronger. The bond contraction has happened globally to adatoms,\textsuperscript{36} dimers,\textsuperscript{37,38} atomic chains,\textsuperscript{31} two-dimensional atomic sheets,\textsuperscript{39,40} nanotubes,\textsuperscript{41} nanoribbons,\textsuperscript{42} atomic vacancies,\textsuperscript{23} terrace edges,\textsuperscript{43} dislocations,\textsuperscript{44} grain boundaries,\textsuperscript{16,35} nanoislands,\textsuperscript{45} liquid skins,\textsuperscript{46} and nanostructures.\textsuperscript{30}

(b) The densely- and tightly-trapped charges will polarize the otherwise conducting electrons such as those in the half-filled s-orbital of metals\textsuperscript{47} or the $\pi$-electrons of sp\textsuperscript{3} hybridized carbon.\textsuperscript{48}

The localized polarization of the $s$-electrons makes Au(4f\textsuperscript{14}5d\textsuperscript{10}6s\textsuperscript{1}), Ru(4d\textsuperscript{7}5s\textsuperscript{1}), Rh(4d\textsuperscript{8}5s\textsuperscript{1}), and Ag(4d\textsuperscript{10} 5s\textsuperscript{1}) nanocrystals nonconductive and magnetic\textsuperscript{5} because the otherwise-conducting electrons become the tightly-locked monopoles, which are expected to play an important role in quantum friction.\textsuperscript{48}

3. DFT calculations

In order to verify the BOLS predictions of the broken-bond-induced quantum trapping and the associated charge polarization, we conducted DFT calculations of the bond length, Mulliken charge transfer in the skins and the valence charge distribution of Au clusters. As the size decreases, metallic NPs will evolve into some distorted structures such as icosahe\textsuperscript{14,49} or decah\textsuperscript{30,51}

Recently, a 49-atom core of a Marks decahedral (MD) structure in a thiol monolayer-protected gold nanoparticle was experimentally confirmed.\textsuperscript{15} However, some researchers claimed that fcc-like cuboctahedral (CO) structures are still stable at small sizes.\textsuperscript{14} Hence, we chose CO13, CO55, CO147 and the MD13, MD49, MD75, as shown in Fig. 1 for our calculations. Nevertheless, the selection of particular structures does not affect the conclusion as we examined the under-coordination effect only. The calculations focus mainly on the change of bond length between atoms of different effective CNs, the charge transfer using Mulliken population analysis, and the energetic distribution of the valence states.

Fig. 1 Gold nanoclusters of cuboctahedral (CO) and Marks decahedral (MD) structures. Indicated numbers are atomic positions in different atomic layers.

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The relativistic DFT calculations were conducted using the DMoP code with a double numeric plus polarization basis set. The DFT semi-core pseudopotential was chosen as approximations for gold, to deal with the core potentials including some degree of relativistic effects. Geometric and electronic structures were obtained on the basis of the localized density approximation in the PW91 form of the functional. During calculations, the self-consistency threshold of the total energy was set at $10^{-8}$ Hartree. The tolerance limit for the energy, forces and displacement in geometry optimizations were set, respectively, at $10^{-5}$ Hartree, 0.002 Hartree/Å and 0.005 Å, respectively.

4. Results and discussion

4.1 Coordination-resolved bond length contraction

As the BOLS theory expected, the spontaneous Au–Au bond contraction at the surface has been confirmed by the current DFT calculations, as listed in Table 1, in addition to the experimental measurements of Huang et al. Using electron cohesive diffraction, Huang and coworkers discovered that the Au–Au bond contraction happens only to the outermost three atomic layers of a gold nanosolid in a radial way, which is further supported by molecular dynamics simulations. The CN dependence of Au–Au bond contraction is insensitive to the type of substrate support. The spontaneous bond contraction depends uniquely on the coordination and has nothing to do with the structural phase or particular elements or the nature of the bond. It has been proven that the equilibrium Au–Au bond in the monatomic chain contracts by 30% from the bulk value of 0.29 nm to 0.20 nm.

In the current DFT geometrical optimization, the bond length of surface Au atoms is shortened with respect to that of the bulk Au atoms (see Table 1). Moreover, Au–Au bonds of the outermost atomic layer, with smaller curvature-dependent CN, shrink more than those in the core interior. The Au–Au distance contracts up to 30%, being in line with experimental observations, as discussed in ref. 56 for Au monatomic chains. The DFT-optimized Au–Au bond lengths follow the trend of the BOLS prediction, but generally, the bond contraction does not reach the derived extent of the BOLS. This quantitative deviation arises from the artifact of the commercial DFT code that needs to include the edge boundary conditions where localized potential depression and charge and energy densification become dominant. Simply inserting a vacuum slab in the calculation may not represent the true situation of edge quantum trapping, which is why we stress the trend consistency between prediction, calculation and measurement throughout the context.

Table 1 Atomic CN-resolved Au–Au bond length $d_i$ (represent the $i^{th}$ shell counting from the outside to the center of the cluster) derived from the DFT geometrical optimization with respect to the bulk standard of $d_0$. The length is in Å. The bond contractions are observed. The charge transfer (Mulliken population analysis) of different structures reveals charge flow from the inner to the outermost atomic shells due to the quantum trapping effect. Negative sign means charge gain otherwise charge loss.

<table>
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<tr>
<th>Structure</th>
<th>Position: atom 1 ~ atom 2</th>
<th>Effective $z_i$</th>
<th>$d_i$</th>
<th>$d_0$</th>
<th>$C_i$ (%)</th>
<th>Shell $i$</th>
<th>Charge Transfer $e$</th>
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<td>CO13</td>
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<td>1</td>
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Fig. 2 (a) Comparison of the BOLS-derived quantum trapping with the mean inner-potential-well depression as a function gold NP size detected by TEM. (b) BOLS reproduction of the size-induced Au 4f core level shift of gold nanostructures on different substrates, which leads to the energy level of an isolated Au atom as 81.505 eV and its bulk shift of 2.865 eV.
core electrons will go deeper, also called the ‘positive core level shift’, that is determined uniquely by the overlap and exchange integrals, or the coupling of the interatomic potential and the specific Bloch wave functions. Excitingly, as shown in Fig. 2(a), TEM measurement has confirmed the size dependence of the muffin-tin inner potential quantum trapping of gold NPs. The mean depth of the inner potential (the volume-averaged electrostatic part of the crystal potential) is increasingly deepened as the diameter of the Au cluster decreases. The trend of inner-potential-well depression is in accordance with the size-induced core level shift. As a result of the surface-potential-well depression, the energy levels of the core electrons will go correspondingly deeper and hence the charge tends to be localized and pinned in the surface layer. The charge transfer of the six considered different nanoclusters is demonstrated (see Table 1) in the calculations using Mulliken charge population analysis. The negative values in Table 1 represents charge gain, and the positive values charge loss. It can be seen that, for the considered structures, the electrons transfer from the inner to the outer shells of the clusters, consistent with the DFT results for Ag nanoclusters.

4.3 Core level shift and valence charge polarization

As a consequence of BOLS, the core-level binding-energy shifts to deeper energies because of the Hamiltonian perturbation. Trapping of the 4f charge with a decrease in size, or thickness, of Au on octane and octanedithiol, Au on TiO$_2$ and on Pt substrates has been observed using X-ray photoelectron emission spectroscopy.

Fig. 2(b) shows the BOLS reproduction of the measured shape and size dependence of the Au 4f core level shift using a least-root-mean-square linearization method, which led to the quantitative information of the 4f energy level of an isolated Au atom as 81.505 eV and its shift of 2.865 eV upon bulk formation. Interested readers are referred to ref. 19 for more details about the calculations and discussion on the surface and size-induced core level shift of a number of samples.

Meanwhile, according to BOLS, the originally conductive s-electrons of Au are expected to be polarized and locally-pinned by the densely- and tightly-trapped core charges. The extent of polarization increases when one goes from the center to the edge with even lower atomic coordination numbers, which is exactly the case of graphene nanoribbons. Au and Ag monomers, dimers, and chain ends. Gold monatomic chains are an ideal prototype for one-dimensional structures and the graphene nanoribbon is an ideal a prototype for two-dimensional structures. They demonstrate the same feature of valence charge polarization at the chain end or at the ribbon edge even though they are different materials. Most strikingly, recent progress revealed that the under-coordinated Pt(5d$^{10}$6s$^0$) and Rh(5s$^1$4d$^8$) adatoms do induce trapped states as additional peaks in the XPS spectra of both the Pt 4f$_{3/2}$ and the Rh 3d$_{5/2}$ energies, but polarization only happens to the Rh adatoms because of the presence of the half-filled Rh 5s electrons. The trapped and polarized states due to adatoms are located, respectively, at energies below and above the bulk component of the XPS spectra.

![Fig. 3](image3.png)  
**Fig. 3** The shell-resolved LDOS for the CO147 and MD75 clusters. The electrons of the outermost shell transfer to the upper edge near the $E_F$ (positioned at 0) while the inner-shell electrons remain at lower energies.

![Fig. 4](image4.png)  
**Fig. 4** Comparison of the resultant valence DOS of all six calculated clusters. The valence charge polarization is more significant in the smaller size, which agrees with the STM/S observations of gold islands of different sizes and from the gold monatomic chain. The STS DOS moves up the most for the smallest island and the polarization is more apparent at the chain end. The convoluted LDOS moves to the upper edge near the $E_F$ (positioned at 0), and the smallest cluster moves most.
stronger polarization effects than the dimer, because the latter has one more coordinated atom.

STM/S investigation shows that the Au–Au chain end atoms exhibit significant polarization near the $E_F$ compared with atoms in the chain interior. Au nanowires of different widths demonstrate that the valence LDOS shifts up and that of the thinnest wire shifts most. The common feature of these experimental observations is that the extent of polarization (energy and density) is more pronounced at sites of even lower-coordinated atoms, which are in good accordance, in trend, with the BOLS expectations and the DFT calculations. The shorter-and-stronger bonds between under-coordinated atoms not only cause local strain, but also quantum trap depression, charge and energy densification, and polarization of the otherwise conducting electrons in the outermost, half-filled, s-orbital of gold.

5. Conclusion

Consistency between the current DFT calculations and the TEM, XPS, and STM/S observations of the size trends of the surface lattice strain, muffin-tin inner potential depression, core level shift, chain end and island charge polarization of gold nanostructures confirmed the predictions made using the BOLS approximation. An incorporation of the BOLS correlation with the DFT calculations and experimental observations has led to a consistent insight into the physical origin of the generation of the strongly localized edge states of gold nanoclusters. The consistency between BOLS expectations and the observed trends of charge localization and the LDOS polarization near the $E_F$ witnesses the significance of the under-coordination, or broken bond. It is particularly emphasized that the under-coordinated atoms are so important that they result in local strain, quantum trap depression, charge densification and valence charge polarization. The understanding herewith and the previously reported observations is that the extent of polarization (energy and density) is more pronounced at sites of even lower-coordinated atoms, which are in good accordance, in trend, with the BOLS expectations and the DFT calculations. The shorter-and-stronger bonds between under-coordinated atoms not only cause local strain, but also quantum trap depression, charge and energy densification, and polarization of the otherwise conducting electrons in the outermost, half-filled, s-orbital of gold.

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